

Explaining incremental models

Workshop on Progressive Data Analysis at IEEE VIS 2024

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Incremental machine learning

Batch machine learning

Given a **set of training data**

$$D = \{(x^1, y^1), \dots, (x^m, y^m) \in X \times Y\}$$

sampled w.r.t. a probability distributions P on $X \times Y$

We aim for a **model** $h : X \rightarrow Y$ such that the error on a test set $T \sim P$

$$E = \sum_{(x,y) \in T} l(h(x), y) \text{ is minimized.}$$



Incremental machine learning

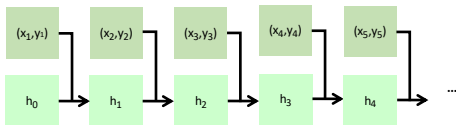
Given a **stream of training data**

$$(x^1, y^1), \dots, (x^t, y^t), \dots \in X \times Y$$

sampled w.r.t. a family of probability distributions P_t on $X \times Y$

We aim for a **learning scheme which incrementally adapts a model**
 $h_t : X \rightarrow Y$ based on (x^t, y^t) such that the interleaved train-test error

$$E = \sum_t l(h_{t-1}(x_t), y_t) \text{ is minimized.}$$



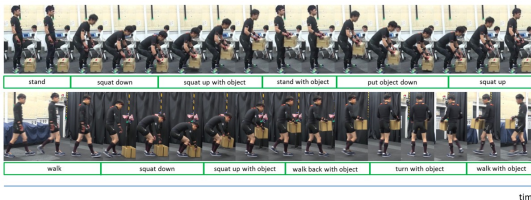
Example: Personalization of models

Data:



<https://www.xsens.com>

- 17 IMUs, 50 Hz, 6 interpolated sensors
- 4 subjects, 9 movements, 10-20 repetitions

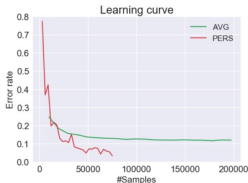


Task:

- predict based on current sensor values
- compare
 - individual online behavior
 - averaged model

Example: Personalization of models

Average vs individual:



Error rate:

Feature set	#Dimensions		AVG	PERS
	AVG	PERS		
Single frame	35	35	0.246	0.172
Stacked	1050	1050	0.190	0.148
DCT	175	175	0.179	0.142

Summaries, models, and data



River



Losing, V., Hasenjäger, M.
A Multi-Modal Gait
Database of Natural
Everyday-Walk in an
Urban Environment. *Sci
Data* 9, 473 (2022).
[https://doi.org/10.1038/
s41597-022-01580-3](https://doi.org/10.1038/s41597-022-01580-3)

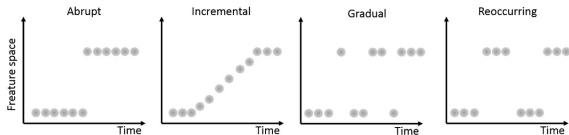
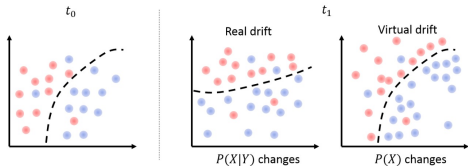
- Jacob Montiel, Max Halford, Saulo Martiello Mastelini, Geoffrey Bolmier, Raphaël Sourty, Robin Vaysse, Adil Zouitine, Heitor Murilo Gomes, Jesse Read, Talel Abdesslem, Albert Bifet: River: machine learning for streaming data in Python. *J. Mach. Learn. Res.* 22: 110:1-110:8 (2021)
- Md. Mahbub Alam, Luís Torgo, Albert Bifet: A Survey on Spatio-temporal Data Analytics Systems. *ACM Comput. Surv.* 54(10s): 219:1-219:38 (2022)
- Viktor Losing, Barbara Hammer, Heiko Wersing: Incremental on-line learning: A review and comparison of state of the art algorithms. *Neurocomputing* 275: 1261-1274 (2018)
- Bartosz Krawczyk, Leandro L. Minku, João Gama, Jerzy Stefanowski, Michal Wozniak: Ensemble learning for data stream analysis: A survey. *Inf. Fusion* 37: 132-156 (2017)
- Gregory Ditzler, Manuel Roveri, Cesare Alippi, Robi Polikar: Learning in Nonstationary Environments: A Survey. *IEEE Comput. Intell. Mag.* 10(4): 12-25 (2015)
- ...

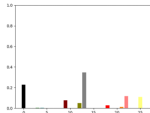
Drift

Drift

Drift is present if there exist time points $t_0 \neq t_1$ such that

$$P_{t_0} \neq P_{t_1}$$





Rialto data set, taken from

V. Losing, B. Hammer and H. Wersing, "KNN Classifier with Self Adjusting Memory for Heterogeneous Concept Drift," 2016 IEEE 16th International Conference on Data Mining (ICDM), Barcelona, Spain, 2016, pp. 291-300, doi: 10.1109/ICDM.2016.0040.

Challenges

- **Drift detection:** identify points in time where the underlying distribution changes (**when?**)
 - **Drift localization:** identify regions in space where the difference of the distribution manifests itself (**where?**)
 - **Drift explanation:** provide intuitive insight about the drift characteristics (**why?**)
- **XAI for drifting scenarios**

Incremental feature importance

Feature importance

Feature importance values:

Given an input space $X = X_1 \times \dots \times X_n$,
given a model $f: X \rightarrow Y$,
given data $D \subseteq (X \times Y)^m$.

Find values $(\lambda_1, \dots, \lambda_n) \in \mathbb{R}^n$
which represent the relevance of the features for the model f and
data D

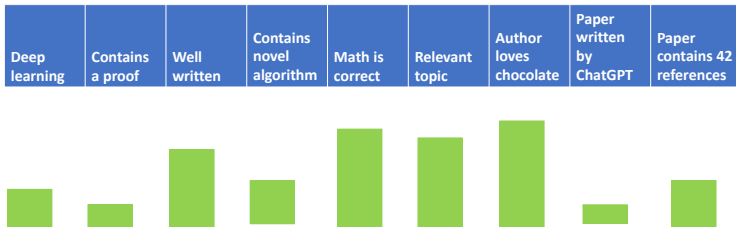
Surveys on properties:

[Degeest, Alexandra ; Fréney, Benoît ; Verleysen, Michel. *Reading grid for feature selection relevance criteria in regression*. In: *Pattern Recognition Letters*, Vol. 148, p. 92-99 (2021) <http://hdl.handle.net/2078.1/250255> -- DOI : 10.1016/j.patrec.2021.04.031]
[A.Bommert, X.Sun, B.Bischi, J.Rahnenführer, M.Lang, Benchmark for filter methods for feature selection in high-dimensional classification data. *Comput. Stat. Data Anal.* 143 (2020)]

Which papers get accepted at a conference?

Deep learning	Contains a proof	Well written	Contains novel algorithm	Math is correct	Relevant topic	Author loves chocolate	Paper written by ChatGPT	Paper contains 42 references	
x				x	x			x	-
	x	x		x	x	x			+
x					x		x		-
	x	x	x	x	x	x			+
x	x	x			x		x	x	-
x		x							-
x		x		x	x	x			+
	x	x	x	x					-
		x		x	x	x			+
x		x		DAV24	x	x		x	+

Feature importance values



Permutation feature importance (PFI)

Deep learning	Contains a proof	Well written	Contains novel algorithm	Math is correct	Relevant topic	Author loves chocolate	Paper written by ChatGPT	Paper contains 42 references	
x				x	x			x	-
	x	x		x	x	x			+
x					x		x		-
	x	x	x	x	x	x			+
x	x	x			x		x	x	-
x		x							-
x		x		x	x	x			+
	x	x	x	x					-
		x		x	x	x			+
x		x		DAV24	x	x		x	+

Permutation feature importance (PFI)

Deep learning	Contains a proof	Well written	Contains novel algorithm	Math is correct	Relevant topic	Author loves chocolate	Paper written by ChatGPT	Paper contains 42 references	
x		x		x	x			x	-
	x			x	x	x			+
x		x			x		x		-
	x		x	x	x	x			+
x	x	x			x		x	x	-
x									-
x		x		x	x	x			+
	x	x	x	x					-
				x	x	x			+
x		x		DAV24	x	x		x	+

Permutation feature importance (PFI)

Permutation feature importance:

Given an input space $X = X_1 \times \dots \times X_n$,
given a model $h: X \rightarrow Y$,
given data $D \subseteq (X \times Y)^m$

Denote a permutation $\varphi: \{1, \dots, m\} \rightarrow \{1, \dots, m\}$.

Permutation feature importance of feature i is given as average over the change of loss when permuting the feature

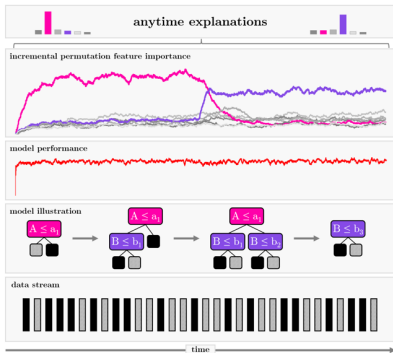
$$\hat{\phi}_\varphi(i) := \frac{1}{m} \sum_j |h(x_1^j, \dots, x_i^{\varphi(j)}, \dots, x_n^j) - y^j| - |h(x^j) - y^j|$$

Incremental feature importance values

Incremental feature importance:

Given a stream of training data
 $(x^1, y^1), \dots, (x^t, y^t), \dots \in X \times Y$
 sampled w.r.t. P_t and incremental
 models $h_t : X \rightarrow Y$

For **every point in time t** , find
 values $(\lambda_1^t, \dots, \lambda_n^t) \in \mathbb{R}^n$
 which represent the relevance of
 the features for the model h_t
 and data sample (x^t, y^t)



Incremental PFI?

time	Deep learning	Contains a proof	Well written	Contains novel algorithm	Math is correct	Relevant topic	Author loves chocolate	Paper written by ChatGPT	Paper contains 42 references	
IEEE VIS	x				x	x			x	-
		x	x		x	x	x			+
	x					x		x		-
NeurIPS		x	x	x	x	x	x			+
	x		x					x	x	-
			x		x	x	x			+
ICML		x	x	x	x					-
			x		x	x	x			+
	x		x		DAV24	x	x		x	+

Permutation feature importance (PFI)

PFI targets

$$\hat{\phi}_{\varphi}(i) := \frac{1}{m} \sum_j |h(x_1^j, \dots, x_i^{\varphi(j)}, \dots, x_n^j) - y^j| - |h(x^j) - y^j|$$

Reliance is the increase in error, averaged over all instantiations of feature i

$$\phi(i) := \sum_j \sum_{j' \neq j} \frac{|h(x_1^j, \dots, x_i^{j'}, \dots, x_n^j) - y^j|}{m(m-1)} - \sum_j \frac{|h(x^j) - y^j|}{m}$$

This can be seen as a **sampling strategy for the marginal distribution** of feature i .

It holds

$$\phi(i) = \frac{m}{m-1} \cdot E_{\varphi \sim \text{unif}(\mathfrak{S}(m))} \hat{\phi}_{\varphi}(i)$$

[Fisher, A.; Rudin, C.; and Dominici, F. 2019. All Models are Wrong, but Many are Useful: Learning a Variable's Importance by Studying an Entire Class of Prediction Models Simultaneously. *Journal of Machine Learning Research*, 20(177): 1–81.]

[Fabian Fumagalli, Maximilian Muschalik, Eyke Hüllermeier, Barbara Hammer: Incremental Permutation Feature Importance (iPFI): Towards Online Explanations on Data Streams. CoRR abs/2209.01939 (2022), Mach. Learn. 112(12): 4863-4903 (2023)]²¹

Incremental PFI (iPFI)

Algorithm 1: iPFI explanation at time t for feature j

Require: $\alpha \in (0, 1)$, sampling strategy φ_t , and $\hat{\phi}_{t-1}^{(S_j)}$.

- 1: **procedure** EXPLAINONE(h_t, x_t, y_t, j)
- 2: $x_s \leftarrow$ **Sample**(φ_t)
- 3: $\hat{\lambda}_t^{(S_j)} \leftarrow \|h_t(x_t^{(S_j)}, x_s^{(S_j)}) - y_t\| - \|h_t(x_t) - y_t\|$
- 4: $\hat{\phi}_t^{(S_j)} \leftarrow (1 - \alpha) \hat{\phi}_{t-1}^{(S_j)} + \alpha \hat{\lambda}_t^{(S_j)}$
- 5: $\varphi_{t+1} \leftarrow$ **UpdateSampler**(φ_t, x_t)
- 6: **end procedure**

run several estimations
of feature relevance in parallel

draw one estimation for x_s
from marginal distribution

take moving average of
relevance estimation

[Fabian Fumagalli, Maximilian Muschalik, Eyke Hüllermeier, Barbara Hammer: Incremental Permutation Feature Importance (iPFI): Towards Online Explanations on Data Streams. CoRR abs/2209.01939 (2022), Mach. Learn. 112(12): 4863-4903 (2023)]

[Maximilian Muschalik, Fabian Fumagalli, Barbara Hammer, Eyke Hüllermeier: Agnostic Explanation of Model Change based on Feature Importance. Künstliche Intell. 36(3): 211-224 (2022)]

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- 5: $\varphi_{t+1} \leftarrow$ **UpdateSampler**(φ_t, x_t)
- 6: **end procedure**

Complete history / uniform sampling:

store all data: x^1, x^2, \dots

store histogram

→ t

Recent history / geometric sampling:

store L data: $x^{i1}, x^{i2}, \dots, x^{iL}$

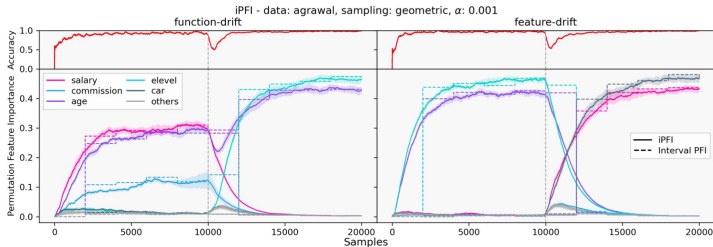
substitutes one
point, $p = \frac{1}{L}$



x^{t+1}

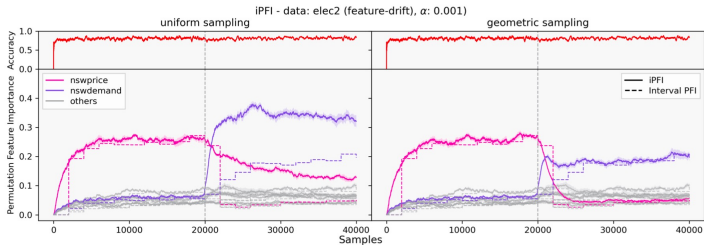
→ t

Incremental PFI (iPFI)



Agrawal data and ARF model: switch concept1 \rightarrow concept2 (left), switch of features (right)

Incremental PFI (iPFI)



Electricity data: uniform (right) versus geometric sampling (right)

Consistency of iPFI

Theorem 2 (Bias for static Model). *If $h \equiv h_t$, then*

$$\phi^{(S_j)}(h) - \bar{\phi}_t^{(S_j)} = (1 - \alpha)^{t-t_0+1} \phi^{(S_j)}(h).$$

Theorem 3 (Variance for static Model). *If $h_t \equiv h$ and $\mathbb{V}[\|h(X_s^{(\bar{S}_j)}, X_r^{(S_j)}) - Y_s\| - \|h(X_s) - Y_s\|] < \infty$, then*

$$\text{Uniform: } \mathbb{V} \left[\lim_{t \rightarrow \infty} \bar{\phi}_t^{(S_j)} \right] = \mathcal{O}(-\alpha \log(\alpha)).$$

$$\text{Geometric: } \mathbb{V} \left[\lim_{t \rightarrow \infty} \bar{\phi}_t^{(S_j)} \right] = \mathcal{O}(\alpha) + \mathcal{O}(p).$$

Incremental XAI toolbox



- compatible with RIVER
- contains
 - iPFI
 - incremental SAGE (Shapley values)

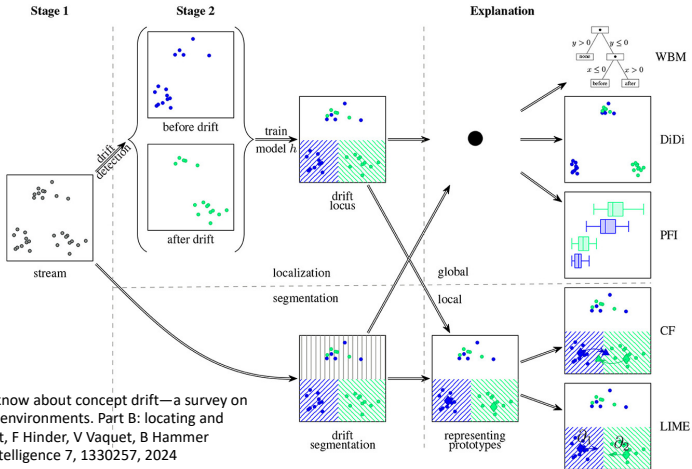


<https://github.com/mmschlk/iXAI>

[Fabian Fumagalli, Maximilian Muschalik, Eyke Hüllermeier, Barbara Hammer: Incremental Permutation Feature Importance (iPFI): Towards Online Explanations on Data Streams. CoRR abs/2209.01939 (2022), Mach. Learn. 112(12): 4863-4903 (2023)]

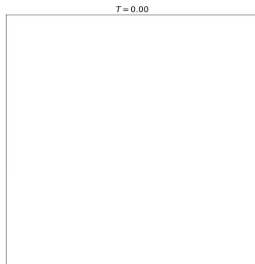
[Maximilian Muschalik, Fabian Fumagalli, Barbara Hammer, Eyke Hüllermeier: iSAGE: An Incremental Version of SAGE for Online Explanation on Data Streams. ECML/PKDD (3) 2023: 428-445]

Model-based drift explanation



One or two things we know about concept drift—a survey on monitoring in evolving environments. Part B: locating and explaining concept drift, F Hinder, V Vaquet, B Hammer
Frontiers in Artificial Intelligence 7, 1330257, 2024

Drift segmentation



- non drifting
- abrupt drift
- abrupt drift (before)
- abrupt drift (after)
- multiple abrupt drifts
- incremental drift
- incremental drift (fast)
- recurring drift

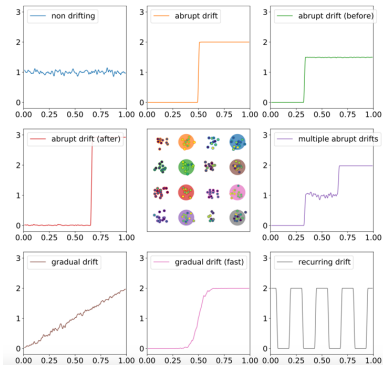
Hinder F., Hammer B.
Concept drift segmentation via Kolmogorov-trees
Verleysen M. (Ed.), ESANN (2021)

Drift segmentation

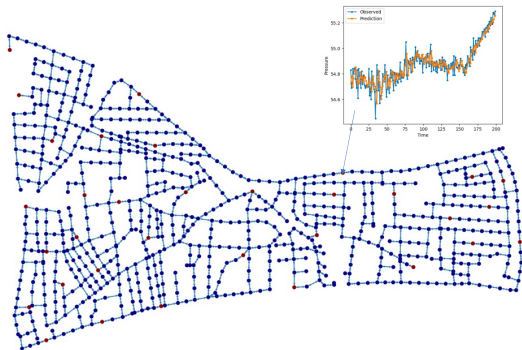
Algorithm:

(ensemble of) decision trees
splits into subsets l_1 and l_2
s.t. difference of $P(T|l_1)$ and $P(T|l_2)$ is
maximum
e.g. using Kolmogorov Smirnov statistics

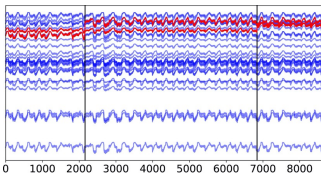
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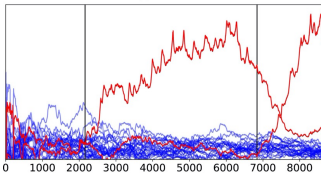
Identification of sensor faults in WDS



Identification of sensor faults in WDS



(a) Raw data



(b) Incremental permutation feature importance

PDAV24

pressure values at
29 locations in the network

Adaptive random forest for
drift segmentation
and iPFI for feature relevance determination

One or two things we know about concept drift—a survey on monitoring in evolving environments. Part B: locating and explaining concept drift, F Hinder, V Vaquet, B Hammer
Frontiers in Artificial Intelligence 7, 1330257, 2024

Take away



Incremental learning enables dealing with drift.

Fast incremental feature relevance determination enables anytime explanation.

Model based drift explanation makes many XAI technologies available

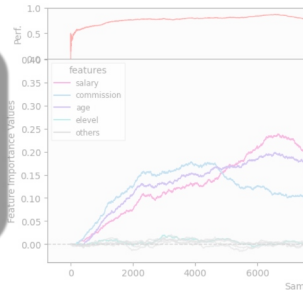
Installation

Examples

Basic Usage

PDAV24

```
pfi_plotter.plot(  
    performance_kw=performance_kw,  
    **fi_kw  
)
```



Thanks to ...

Fabian Fumagalli, Martina Hasenjäger, Fabian Hinder,
Eyke Hüllermeier, Viktor Losing, Maximilian Muschalik,
Valerie Vaquet, Heiko Wersing, Taizo Yoshikawa



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